

q	x	f	fx	$(x - \bar{x})$	$f(x - \bar{x})^2$
	300,000	2	600,000	-925,000	1.711×10^{12}
	500,000	3	1,500,000	-725,000	1.577×10^{12}
	750,000	8	6,000,000	-475,000	1.805×10^{12}
	900,000	6	5,400,000	-325,000	6.63×10^{11}
	1,000,000	2	2,000,000	-225,000	1.0125×10^{11}
	1,500,000	1	1,500,000	275,000	7.5×10^{10}
	3,000,000	1	3,000,000	1,775,000	3.15×10^{12}
	4,000,000	1	4,000,000	2,775,000	7.7×10^{12}
		24	29,400,000		1.554×10^{13}

(9)

$$\frac{\sum fx}{24} = \frac{29,400,000}{24}$$

$$1,225,000$$

Interquartile Range:

$$Q_1 = \frac{1}{4} \times 25 = \frac{25}{4} = 6.25$$

$$= 750,000$$

$$Q_3 = 6.25 \times 8 = 18.75$$

$$900,000$$

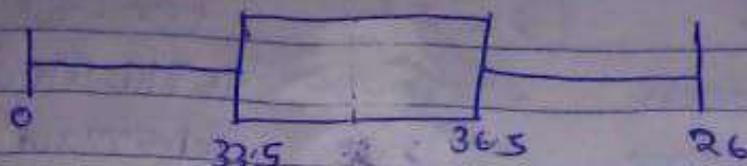
$$Q_3 - Q_1 = 900,000 - 750,000$$

$$150,000$$

Same quartile range

$$\frac{150,000}{2} = 75,000$$

c



(8)

(a) The standard deviation will be about smaller and hence, left hand whisker will be shorter

$$(b) \frac{12 + 160 + 245 + 304}{21} = \frac{721}{21}$$

$$34.4$$

The new mean is ~~37.4~~ 34.4

(c) This is due to the removal of outliers

10 Chi-Yan have better control over her drives & a lower standard deviation in their distances. If their putting abilities are essentially equal, then Chi-Yan will more likely to have a better score in a round of golf.

Standard deviation

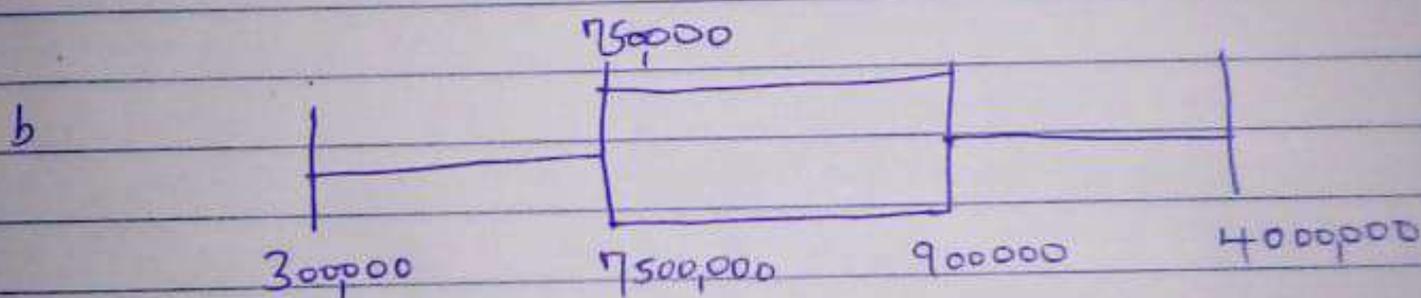
Variance

$$s^2 = \frac{1.554 \times 10^{13}}{24} = 6.475 \times 10^{11}$$

Standard deviation

$$\sqrt{6.475 \times 10^{11}}$$

$$= 804\,673$$



$$(c) \quad Z \text{ score} = \frac{300,000 - 1,225,000}{804,673}$$

$$= -0.87$$

(d) After calculating the new average salary and standard deviation, the Z-score will be -0.037 .

$$\frac{18-20}{4.06} = \frac{-2}{4.06} = -0.49$$

$$\frac{15-20}{4.06} = \frac{-5}{4.06} = -1.23$$

$$\frac{26-20}{4.06} = \frac{6}{4.06} = 1.48$$

$$\frac{20-20}{4.06} = \frac{0}{4.06} = 0$$

$$\frac{21-20}{4.06} = \frac{1}{4.06} = 0.25$$

6. mean

$$44 + 18 + 125 + 80 + 63 + 42 + 35 + 68 + 52 + 75 + 260 + 96 + 110 + 72 + 51$$

$$\frac{1191}{15} = 79.5$$

$$44 - 79.5 = -35.5 = 1260.25$$

$$18 - 79.5 = -61.5 = 3782.25$$

$$125 - 79.5 = 46.5 = 2162.25$$

$$80 - 79.5 = 0.5 = 0.25$$

$$63 - 79.5 = 16.5 = 272.25$$

$$42 - 79.5 = -37.5 = 1406.25$$

$$35 - 79.5 = -44.5 = 1980.25$$

$$68 - 79.5 = -11.5 = 132.25$$

$$52 - 79.5 = -27.5 = 756.25$$

$$75 - 79.5 = -4.5 = 20.25$$

$$260 - 79.5 = 180.5 = 32580.25$$

$$96 - 79.5 = 16.5 = 272.25$$

$$110 - 79.5 = 30.5 = 930.25$$

$$72 - 79.5 = -7.5 = 56.25$$

$$51 - 79.5 = -28.5 = 812.25$$

$$\text{Total } 46304.75$$

variance:

$$s^2 = \frac{46,304.25}{15-1} = 3307.45$$

standard deviation

$$\sqrt{3307.45} \\ = 57.51$$

(b) Median

18: 35, 42, 44, 51, 52, 63, 65, 72, 75, 80, 96, 110, 125, 260

$$\frac{1 \times 18 + 1}{2} = \frac{1 \times 16}{2} = 8^{\text{th}} \\ = 68$$

Interquartile range:

$$Q_1 = \frac{1 \times 16}{4} = 44$$

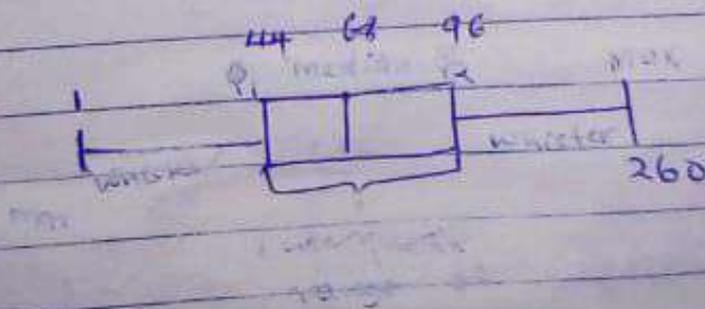
$$Q_3 = \frac{3 \times 16}{4} = 12^{\text{th}} = 96$$

$$96 - 44 = 52$$

Semi quartile

$$\frac{52}{2} = 26$$

(c)



(d) 260

Variance

$$s^2 = \frac{945.91}{9}$$

$$= 108.35$$

Standard deviation

$$\sqrt{108.35}$$

$$= 10.41$$

(2)

(a) 3, 4, 5, 6, 8, 9, 11, 15

$$\text{median} = 6$$

$$Q_1 = \frac{1}{4} \times 10 = 2.5$$

between 2nd and 3rd

$$\frac{4+5}{2} = 4.5$$

$$Q_3 = \frac{3}{4} \times 10 = 7.5$$

between 7th and 8th

$$\frac{9+11}{2} = 10$$

Interquartile range

$$10 - 4.5$$

$$= 5.5$$

(3)

43, 48, 56, 59, 62, 64, 67, 71, 72, 75, 75, 78, 81, 84, 88, 90

$$\text{Median} = \frac{1}{2} \times 17 = 8.5$$

$$\frac{71+72}{2} = 71.5$$

7(a) Mean

X	f	cf	fx	X-2	f(x-2) ²
12	1	1	12	-23.8	566.44
32	5	6	160	-3.8	14.44
25	7	13	245	-0.8	0.64
38	8	21	304	2.2	4.84
42	5	26	210	6.2	38.44
	26		931		874.04

mean

$$\frac{\sum fx}{\sum f} = \frac{931}{26}$$

$$35.8$$

$$\text{Variance} = \frac{874.04}{26}$$

$$33.6$$

$$\text{Standard deviation} = \sqrt{33.6}$$

$$= 5.8$$

(b) median

$$\frac{26+1}{2} = 13.5 = 13^{\text{th}} \text{ and } 14^{\text{th}}$$

$$\frac{38+35}{2} = \frac{73}{2} = 36.5$$

Interquartile

$$Q_1 = \frac{13.5}{2} = 6.75 = 6^{\text{th}} \text{ and } 7^{\text{th}}$$

$$\frac{32+35}{2} = 33.5$$

$$Q_2 = 6.75 \times 3 = 20.25 = \frac{38+35}{2} = \frac{73}{2} = 36.5$$

$$Q_3 = 36.5 - 33.5$$

$$3$$

Semiinterquartile

$$\frac{3}{2}$$

$$= 1.5$$

$$Q_1 = \frac{59 + 62}{2} = 60.5$$

$$Q_3 = \frac{78 + 81}{2} = 79.5$$

Interquartile range

$$79.5 - 60.5$$

$$= 19$$

(3)

(a) First quartile

(b) Second quartile

(c) Second quartile

4

(a) 25th or 25%

(b) 50th or 50%

(c) 75th or 75%

5)

$$18 + 15 + 26 + 20 + 21$$

$$= \frac{100}{5} = 20$$

$(x - \bar{x})^2$

$$S = \sqrt{\frac{66}{5-1}}$$

$$= \sqrt{16.5} = 4.06$$

$$18 - 20 = -2 = 4$$

$$15 - 20 = -5 = 25$$

$$26 - 20 = 6 = 36$$

$$20 - 20 = 0 = 0$$

$$21 - 20 = 1 = 1$$

$$\frac{1}{66}$$

2.6

1.20

Mean

$$5+7+9+6+5+10+8+2+11+8+7+9+6+9+5+8$$

$$\frac{\sum X}{N} = \frac{113}{16} = 7.0625$$

Standard deviation: Variance

$$S = \sqrt{\frac{\sum (X - \mu)^2}{N}}$$

$$5 - 7.1 = (-2.1 \times 3) = -2.1 \times 3 = -6.3 \Rightarrow (-6.3)^2 = 39.69$$

$$7 - 7.1 = (-0.1 \times 3) = -0.3 \Rightarrow (-0.3)^2 = 0.09$$

$$9 - 7.1 = (1.9 \times 2) = 3.8 \Rightarrow 3.8^2 = 14.44$$

$$8 - 7.1 = (-1.1 \times 2) = -2.2 \Rightarrow (-2.2)^2 = 4.84$$

$$10 - 7.1 = (2.9 \times 1) = 2.9 \Rightarrow 2.9^2 = 8.41$$

$$8 - 7.1 = (0.9 \times 3) = 2.7 \Rightarrow 2.7^2 = 7.29$$

$$2 - 7.1 = (-5.1 \times 1) = -5.1 \Rightarrow (-5.1)^2 = 26.01$$

$$11 - 7.1 = (3.9 \times 1) = 3.9 \Rightarrow 3.9^2 = 15.21$$

Total 160.26

$$\sigma^2 = \frac{160.26}{16}$$

$$= \frac{10.01625}{1}$$

$$= 5.0$$

Standard deviation

$$\sigma = \sqrt{5}$$

$$= 2.2$$

(b)

mean: $12.55 + 15.31 + 21.98 + 45.35 + 19.81 + 33.89 + 29.53 + 30.19 + 38.20$

$$\frac{246.81}{9} = 27.42$$

$$12.55 - 27.42 = (-14.87) \Rightarrow 221.12$$

$$15.31 - 27.42 = (-12.11) \Rightarrow 146.65$$

$$21.98 - 27.42 = (-5.44) \Rightarrow 29.59$$

$$45.35 - 27.42 = (17.93) \Rightarrow 321.48$$

$$19.81 - 27.42 = (-7.61) \Rightarrow 57.91$$

$$33.81 - 27.42 = (6.39) \Rightarrow 40.83$$

$$29.52 - 27.42 = (2.11) \Rightarrow 4.45$$

$$30.19 - 27.42 = (2.77) \Rightarrow 7.67$$

$$38.20 - 27.42 = (10.78) \Rightarrow 116.20$$

Total: 945.91